

Assignment 2

- Published: *Feb 11*
- Deadline: *March 4*
- Implement backpropagation for a neural network
- Find hyperparameters for optimization and generalization



$$L = \text{cross-entropy}(y_1, \dots, y_K)$$

Softmax probabilities

$$y_k = \text{softmax}(o_1, o_2, \dots, o_K)$$



Input to softmax

$$o_k = \sum_{j=1}^J v_{jk} h_j$$



Hidden units

$$h_j = \text{logistic}(z_j)$$

I: # input units
J: # hidden units
K: # output classes



Input to hidden units

$$z_j = \sum_{i=1}^I w_{ij} x_i$$



Input

$$x_i$$

Use chain rule to backpropagate gradients

Hidden to output weights:

$$\frac{\partial L}{\partial v_{jk}} = \frac{\partial L}{\partial o_k} \frac{\partial o_k}{\partial v_{jk}}$$

Input to hidden weights:

$$\frac{\partial L}{\partial w_{ij}} = \sum_{k=1}^K \frac{\partial L}{\partial o_k} \frac{\partial o_k}{\partial h_j} \frac{\partial h_j}{\partial z_j} \frac{\partial z_j}{\partial w_{ij}}$$

To Do, possible snags, and tips

- derive specific expressions for gradients
- derive expressions on paper before implementing them
- compute gradients for multiple training cases
- check specific expression for loss function, average gradients over minibatch
- vectorize expressions
- make use of gradient checker (not a guarantee for correct gradients but helpful)
- Helpful material:
 - Backprop video (Lecture 3d)
 - [Backprop example](#)
 - Code from Jan 23 tutorial
- Read assignment carefully